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TRAJECTORY ANALYSIS OF
A RADIAL HOMING GLIDING PARACHUTE
IN A UNIFORM WIND

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Arthur L. Murphy, Jr.

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I-B

Abstract continued.

a limacon. An optimum launch point is established from this result. When a fixed flight time is specified, the locus of points of equal time to the target is shown to be an ellipse. This determines the release path for the case of multiple delivery from a single launch vehicle.

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TRAJECTORY ANALYSIS OF A RADIAL

HOMING GLIDING PARACHUTE IN A UNIFORM WIND

by

Arthur L. Murphy Jr.

September 1971

Airdrop Engineering Laboratory
US Army Natick Laboratories
Natick, Massachusetts

I-D

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This report presents an analytic assessment of one type of steering law used to control the trajectory of gliding decelerators. The analysis is part of a continuing effort directed toward investigating methods which will improve the accuracy and dispersion characteristics of airdrop systems.

This study was conducted under Department of the Army Project No. 1F1 62203 AA33, Drop Zone Dispersion Studies.

NOMENCLATURE

r = Magnitude of the radius vector in polar coordinates

t = Time

U = Vector component of the parachute's total airspeed vector in the horizontal plane

u = Magnitude of U

w = Magnitude of the wind speed vector W

x = Horizontal space coordinate fixed to earth

y = Horizontal space coordinate perpendicular to x and fixed to earth

λ = u/w wind penetration parameter

θ = Azimuth angle in polar coordinates

Subscripts

1 = Launch

m = Minimum

TABLE OF FIGURES

ABSTRACT

The two dimensional trajectory of a radial homing gliding parachute in a uniform wind is presented. The kinematics of the motion is discussed generating two first order differential equations which are separated and solved by direct integration. The resulting expression functionally relates the radial position of the parachute to the instantaneous value of the azimuth angle. Utilizing this result, an exact solution for time in terms of space coordinates is then obtained. From geometric considerations, the angular motion along the azimuth direction is found to be stable when the system is flying into the wind. The trajectory equation shows that under the radial guidance constraint, a gliding system without wind penetration ability can never pass directly over the intended point of impact. However, when the system's glide capability is greater than that of the wind, the parachute has the potential of always reaching the target, provided there is sufficient flight time. In this glide region, the total time to the target as a function of launch angle relative to the wind line, generates the plane curve of a limacon. An optimum launch point is established from this result. When a fixed flight time is specified, the locus of points of equal time to the target is shown to be an ellipse. This determines the release path for the case of multiple delivery from a single launch vehicle.

INTRODUCTION

The most severe limitation on parachute delivery is its
inherent inaccuracy. Descending as a static entity in an
environment which cannot be controlled or precisely predicted,
the parachuted load impacts essentially where the wind directs
it. Investigators, both private and government sponsored,
recognizing the constraint imposed by the passive role of
the standard decelerator, have developed highly maneuverable
gliding canopies capable of penetrating winds in excess of
twenty five knots. In addition to their aerodynamic qualities
these flexible wings can be stowed and deployed according to
standard parachute methodology and thereby retain the desirable
packaging feature of conventional designs.

Deceleration systems, employing gliding canopies, have
been extensively investigated in research and development
programs by both military and space agencies. In general,
the utilization of unmanned gliding systems for military
airdrop or for providing the terminal stage air transport
of re-entry vehicles, requires guidance and control equipment.
Radio control guidance systems have been developed for military
airdrop applications,[1] and have been proposed for use in
sounding rocket payload retrieval.[2]

In these systems the parachute's direction of flight is
controlled through a servo mechanism rigged to the suspension
lines of the canopy. Left or right constant rate turns are

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produced by retracting the appropriate control line. The
communication which activates the control and steers the
system is provided by a radio transmitter located at the
intended impact point, and a receiver with two antennas,
positioned on the suspended load. The antennas are physically
separated and are located on the load, so as to define a
plane which is perpendicular to the horizontal projection of
the parachute's total airspeed vector. With this arrangement,
signals emanating from the transmitter will appear equal in
magnitude to the separate antennas only when the system's
velocity vector is aligned with a radial path connecting it
and the target. For any other orientation, a disparity in
signal strength is perceived which activates a control,
producing a rotation of the parachute towards the ground
based transmitter. The wind acting in conjunction with
some over control, continually disturbs the system from
fixing on a straight line course causing the parachute to
steadily maneuver as it seeks radial alignment. This motion
which effectively produces what might be termed a radial
homing maneuver, persists throughout the flight or until the
load passes directly over the transmitter. Upon passing over
the target the system executes an orbital path about the
transmitter until impact.

This paper treats the approach portion of the trajectory
of a radial homing gliding parachute in a uniform wind.
Exact solutions completely determining the path in terms of

time and space coordinates are obtained. A detailed analysis
of these equations is made leading to a comprehensive
assessment of gliding parachute capability when operating in
a uniform wind and constrained by radial homing. Previous
efforts dealing specifically with wind effects upon gliding
systems have been carried out on a numerical basis and are
contained in References 3 and 4. An independent analytic
treatment similar in scope and applied to determining the
time required for an aircraft to execute a round trip in a
uniform wind, may be found in Reference 5.

EQUATIONS FOR RADIAL GUIDANCE

Analysis

Figure 1a depicts the essential geometric aspects of a
radial homing gliding parachute in a uniform wind. The wind
speed is taken to be steady, to lie entirely in the x-y plane,
and to point along the y axis in a negative sense. There is
no loss of generality in the arbitrary alignment of the wind
line with the y direction, since any other selection merely
constitutes a rotation of the resulting trajectory relative
to this coordinate axis.

Under equilibrium conditions, the magnitude of the
parachute's velocity relative to the air mass remains constant.
The lift to drag ratio is fixed, thereby, specifying the
vertical and horizontal projections of the total airspeed
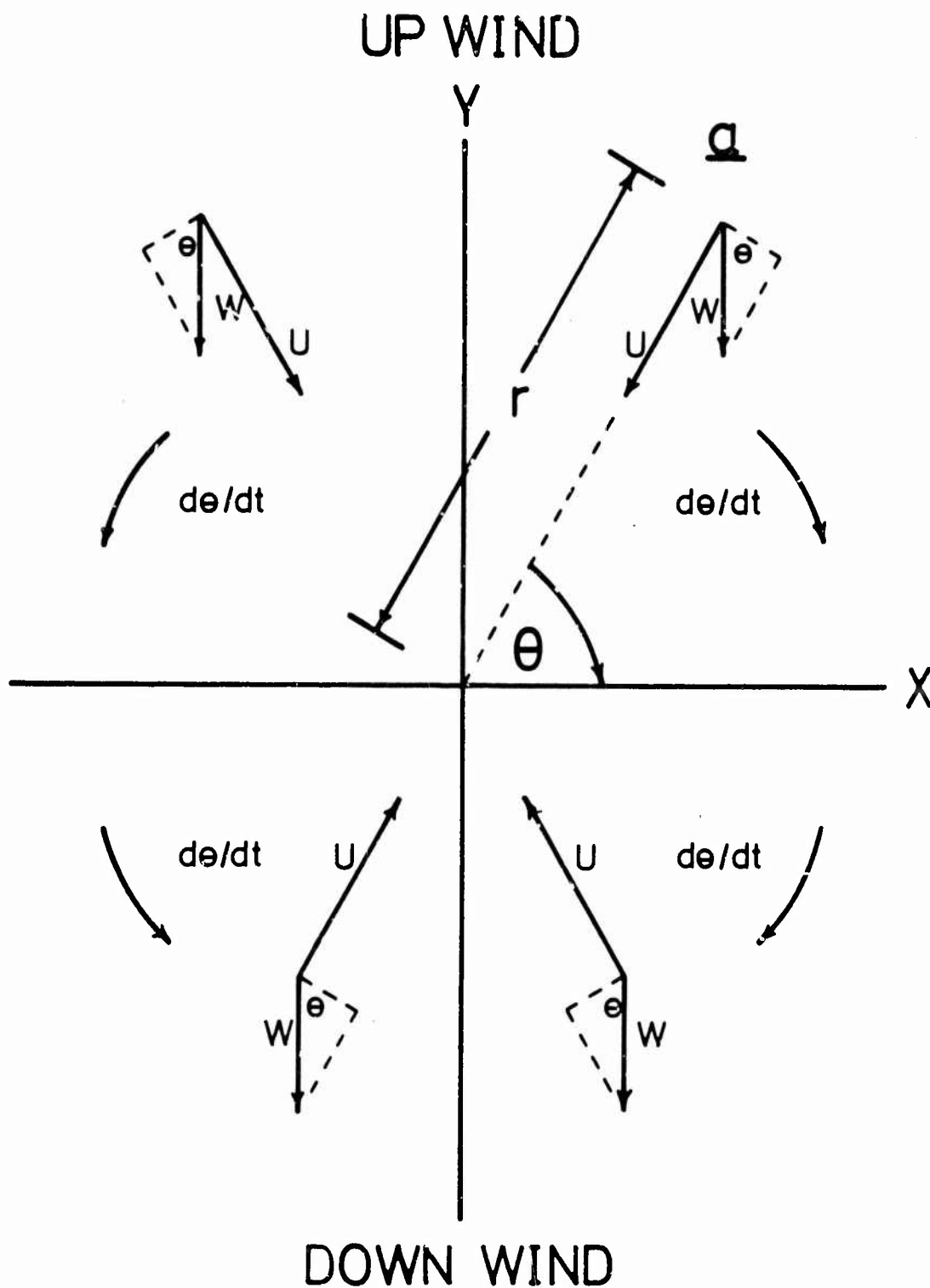vector. It is assumed that the physical act of deflecting a

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FIGURE 1. THE KINEMATICS OF RADIAL HOMING

control line serves to change only the direction of the
horizontal velocity component while leaving the vertical vector
undisturbed. The motion is, therefore, separated with the
vertical mode one of steady descent. As a consequence, the
problem becomes a two-dimensional one where the radial guidance
constraint reacting to the presence of the wind, forces U the
airspeed vector in the horizontal plane, to assume a continuous
orientation in the negative radial direction. Operationally,
this motion that is idealized by steady modulation of the
control, approximates a series of discrete actions combining
left and right turns with periods of straight flight.

Within the constraints specified then, the fundamental
relationship describing the motion can now be stated as a
vector equation relating the absolute velocity of the system
relative to an earth fixed reference, to the sum of the wind
velocity and the horizontal component of the parachute
airspeed vector U. Expressed in polar coordinates the
scalar equations obtained from this vector equality are:

$$dr/dt = -(w\sin\theta+u), \tag{1}$$

and

$$(r)d\theta/dt = -w\cos\theta. \tag{2}$$

Stability Characteristics of the Wind Line

Before attempting to obtain solutions from equations
(1) and (2), some immediate information regarding the nature

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of the angular motion of the parachute with respect to the
wind axis can be found directly by examination of equation
(2) in conjunction with figure 1. From (2) it is seen that
$d\theta/dt < 0$, thereby, requiring θ to be a decreasing variable.
The physical ramifications of this observation can be appreciated
by noting again from equation (2) that the angular velocity
of the system relative to the fixed reference is due entirely
to the wind with no contribution from the vector U. At
locations then on the upwind side, that is, coordinate positions
where y is a positive, this component of the wind velocity
will continually increase any misalignment between the wind
line and the vector U. On the down-wind side, $(y < 0)$, angular
alignment will be reinforced by this action of the wind.
Consequently, and as a figure 1 shows, approaches made along
the wind axis from a down-wind position will be insensitve to
nominal heading disturbances and are, therefore, stable while
the converse is true for the upwind case. Hence, a gliding
system which is executing a radial steering maneuver in somewhat
steady atmospheric conditions naturally seeks and maintains
alignment into the wind. This property, that exists at least
in theory, enhances the potential application of gliding
decelerators, particularly when consideration is given to
the problem of reducing and cushioning the horizontal velocity
prior to and during impact.

Trajectory Determination

Turning now to equation (1) and (2) the r and θ variables may readily be separated to give;

$$dr/d\theta = r(\tan\theta + \lambda\sec\theta); \tag{3}$$

Where $\lambda = u/w$ is defined as the wind penetration parameter. The expression given in (3) can now be integrated directly yielding:

$$r = K\sec\theta(\sec\theta + \tan\theta)^{\lambda}; \tag{4}$$

Where K, the constant of integration, is given by:

$$K = r_1/\sec\theta_1(\sec\theta_1 + \tan\theta_1)^{\lambda}. \tag{5}$$

The basic formulation and subsequent solution to (3) assumes initial alignment along a radial at some angular offset from the wind line. To apply (3) the initial or launch position will be selected to lie along a ray between $\pm$ 90 degrees. The situation of perfect alignment along the wind axis at launch is a special case and cannot be handled directly with (3). Evaluation of this particular condition is made directly in (1) by requiring θ to be 90 degrees. The resulting solution is the physical case where the parachute either closes with, remains stationary, or departs from the target along a straight line path coincident with the wind line.

A rectangular form for equation (4) can be obtained by defining:

$$p = x/k, \qquad (6)$$

and

$$q = y/K. \qquad (7)$$

Making the appropriate substitutions in (4) yields:

$$q = (1/2)\{p^{(\lambda+1)/\lambda} - p^{(\lambda-1)/\lambda}\}. \qquad (8)$$

For the special case of $\lambda = 1$ this expression reduces to:

$$q = (1/2)(p^2 - 1). \qquad (9)$$

Hence, when the wind speed is equal in magnitude to the parachute's horizontal airspeed component u, the ground track of a radial homing gliding system will be parabolic. This result will be seen to be of practical significance when trajectories with larger values of λ are examined.

It is now possible to obtain an integral relationship for time by combining equation (2) with the expression in (4). This gives:

$$t = (-K\lambda/u)\int \sec^2\theta(\sec\theta+\tan\theta)^\lambda d\theta. \qquad (10)$$

Equation (10) can be integrated by parts to give the general expression for time;

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$$t = \{\lambda/u(\lambda^2-1)\}\{r_1(\lambda-\sin\theta_1)-r(\lambda-\sin\theta)\}. \qquad (11)$$

However, for the special case of $\lambda = 1$, (11) does not hold requiring evaluation directly from (10). Thus when $\lambda = 1$;

$$t = (-K\lambda/2u)\{\sec\theta(\sec\theta+\tan\theta)+\ln(\sec\theta+\tan\theta)\}\Big|_{\theta_1}^{\theta}. \qquad (12)$$

At this point, the trajectory of a radial homing gliding parachute operating in a uniform wind is completely specified by equations (4), (5), (11), and (12).

TARGET LIMITS WITH RADIAL HOMING

The Case of $\lambda < 1$.

Equation (4) is graphically represented in figure (2) for the circumstance where $\lambda < 1$. A unit launch radius is assumed and curves are generated for a selected value of the initial azimuth angle. The nature of these curves indicate that r never becomes zero. Instead, the path lines appear to bend away causing the parachute to pass through what appears to be a minimum radial position relative to the aiming point.

The first of these observations can be verified directly by examining equation (4) when r is required to be zero. This leads to the expression;

$$0 = \{(1+\sin\theta)^{\lambda-1}/(1-\sin\theta)^{\lambda+1}\}^{1/2}. \qquad (13)$$

This relationship cannot be satisfied when $\lambda < 1$ for values of θ in the range, $-90 \le \theta < 90$ degrees. Consequently, r can never be zero when $\lambda < 1$.
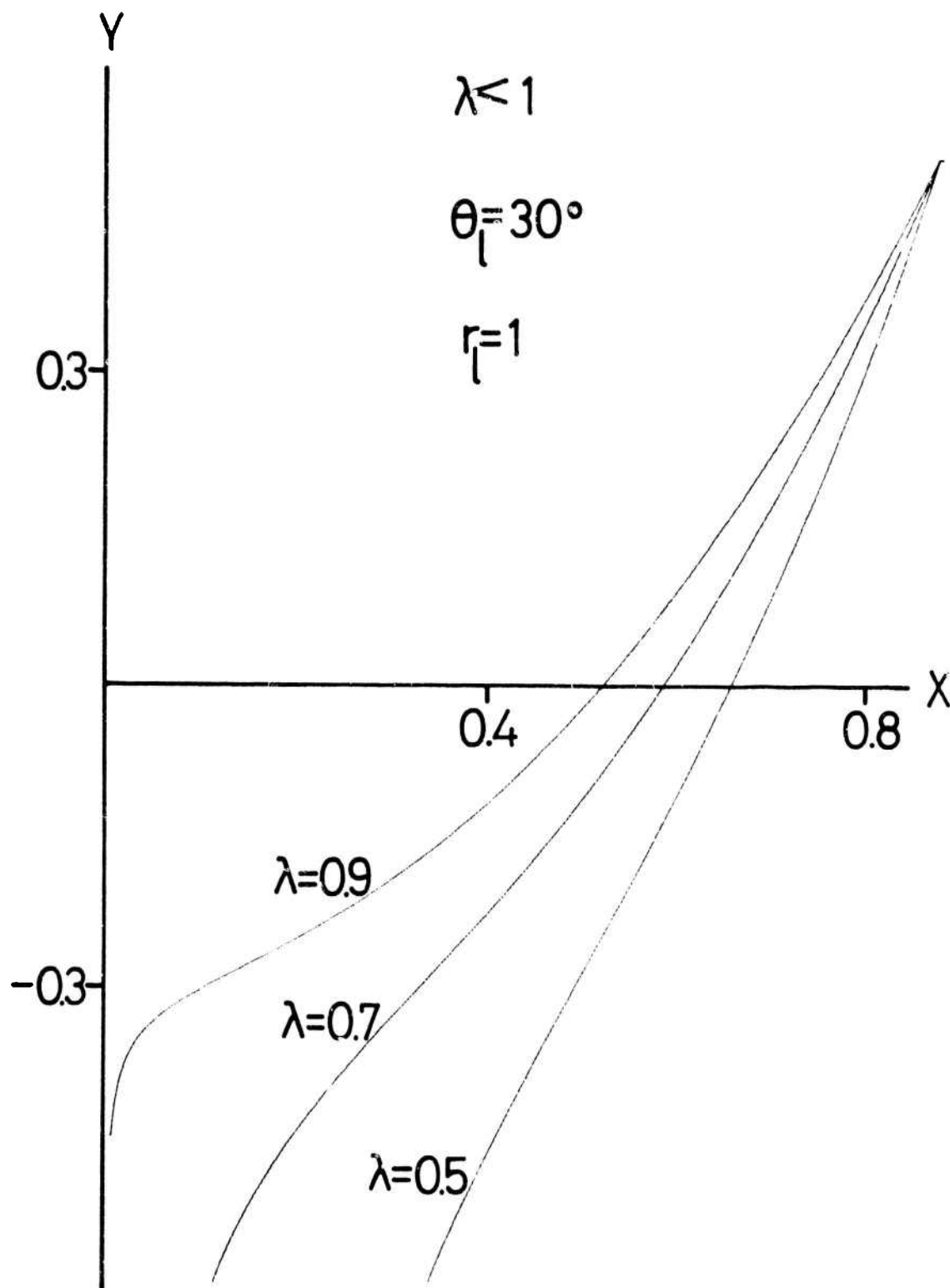
FIGURE 2: RADIAL HOMING TRAJECTORIES WHEN λ<1.

The existence of an extremum can now be investigated by applying maxima and minima theory of differential calculus to (4). That is, $dr/d\theta$ is set equal to zero yielding the requirement that:

$$\text{either } r = 0, \tag{14}$$

$$\text{or } \sin\theta = -\lambda . \tag{15}$$

The first of these results has been previously dealt with thereby designating (15) as the appropriate condition. Since (15) can be satisfied for λ between 0 and 1 the existence of a relative minimum r has been verified. The magnitude of the minimum radius can now be evaluated as;

$$r_m = \{K/(1-\lambda^2)^{1/2}\}\{1-\lambda/1+\lambda\}^{\lambda/2} ; \tag{16}$$

$$\text{When } \theta = \theta_m = \text{Arc sin } (-\lambda) . \tag{17}$$

The velocity components at this position are given by;

$$dr/dt = 0, \tag{18}$$

$$\text{and } (r)d\theta/dt = -w(1-\lambda^2)^{1/2} . \tag{19}$$

Equations (16) and (17) completely designate what might be called the perigee of the homing orbit when $\lambda < 1$. However, some restrictions are in ord λ concerning the application of (16) regarding the quantity K. The constant of integration K is seen, from (5) to be a function of θ_1 as well as λ .

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Intuititively, it would be expected that for fixed values of λ, r_m would tend to increase as θ_1 takes on values further away from the 90 degree ray. This will be true in (16) up to the point where;

$$\theta_1 = \text{Arc sin } (-\lambda) . \tag{20}$$

Beyond this condition (i.e. launch angles less than those given by equation (20)) the equality required in (15) cannot be met, since, θ being a decreasing variable prevents counter clockwise rotations. Physically then, there will be no relative minimum point along the path when $\theta_1 < \text{Arc sin } (-\lambda)$ and, a system launched at these coordinates will be on a course of ever increasing radius.

From the treatment thus far, some conclusions regarding the accuracy potential of radial homing systems is apparent. A gliding system with $\lambda < 1$ can never fly directly over the target. Its closest penetration will be given by (16) provided the launch is effected such that $\theta_1 \geq \text{Arc sin } (-\lambda)$. If this condition is not met the parachute will be on a divergent path with the launch radius (r_1) its minimum point relative to the target.

The Case of $\lambda \geq 1$.
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Much of the previous analysis has laid the foundation for treating this particular case. Returning to equation (13)

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it is seen that when $\theta = -90$ degrees, r will be zero for all values of $\lambda > 1$. The requirement in (14) is now met, thereby establishing the obvious fact that r = 0 is a minimum. Figure (3), which is a plot of equation (4), visually verifies these observations again, for the conditions of a unit launch radius and a selected initial angular coordinate.

From Figure (3) it is noted that the parabolic path (the special case of $\lambda=1$), provides a border to all trajectories with higher values of λ launched from the same position. Extending the tail of this reference parabola effectively produces a boundary containing all paths initiated at the nominal reference radius and at some angular coordinate between the wind line and the selected reference angle. The impact points of all radial homing systems launched under these conditions will be found interior to the envelope defined by the reference parabola and the wind axis. If then, equation (12) is utilized, the above definition of required drop zone area can be further refined.

In summary then, the analysis of the case where $\lambda > 1$ has demonstrated that a radial homing gliding system with some wind penetration ability, has the potential of always reaching the target provided there is sufficient flight time. It has also been shown, through equation (13), that ideally the system will achieve alignment into the wind the moment it arrives over the target. This, of course, is the
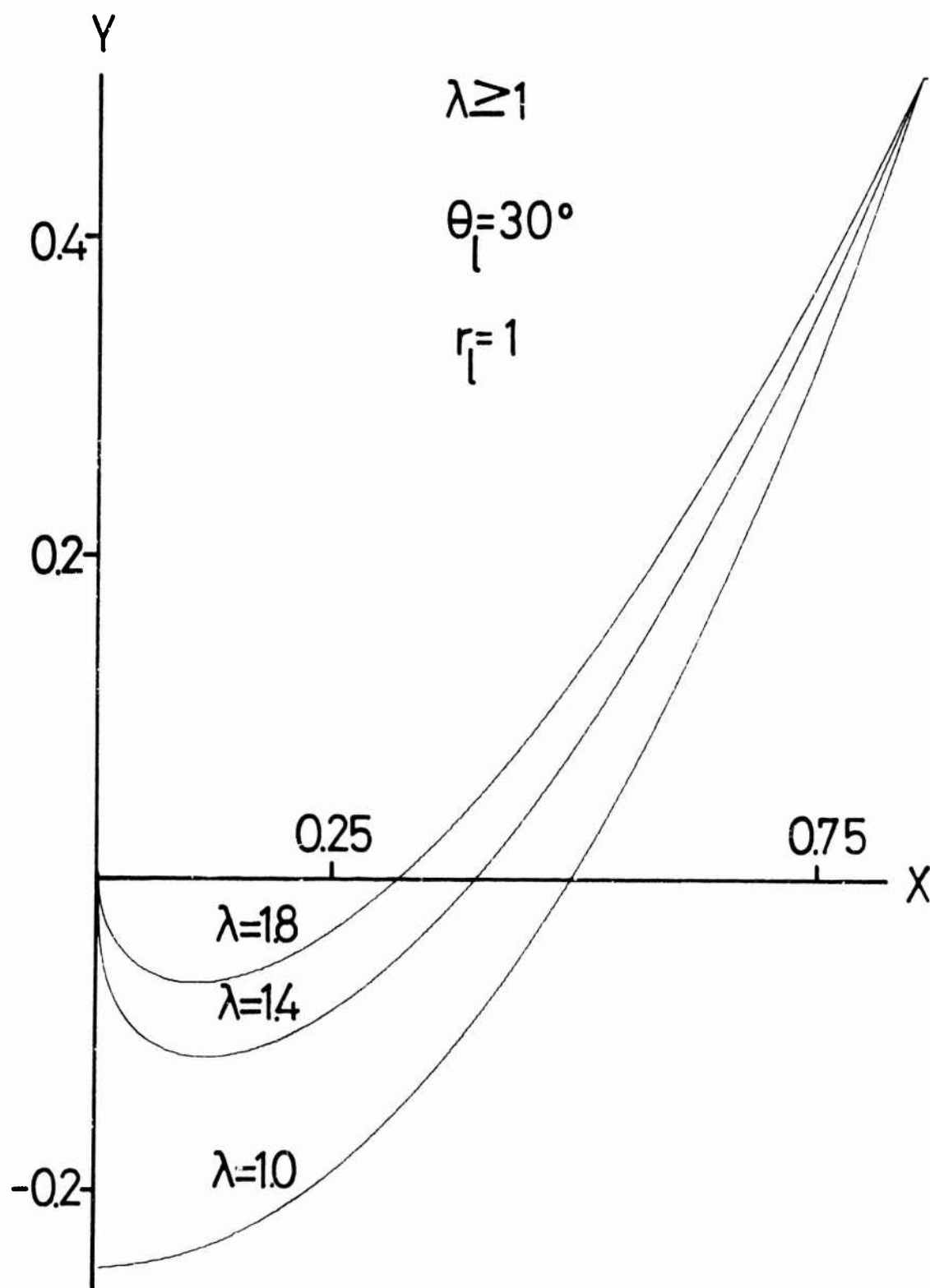
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FIGURE 3: RADIAL HOMING TRAJECTORIES WHEN λ≥1

optimum landing configuration for considerations of impact.
The special circumstance where $\lambda = 1$, the case of a parabolic
path, is seen to provide a tool for estimating the required
drop area when certain nominal launch conditions are specified.

LAUNCH CRITERIA

Fixed Radius of Launch

Turning now to equation (11), flight time requirements
for radial homing gliding systems will be investigated for
the case where $\lambda > 1$. Target acquisition implies the physical
attainment of coordinates $r = 0$, and $\theta = -90$ degrees.
Imposing these conditions on (11) yields:

$$ut/r_1 \underset{\Delta}{=} \tau = (\lambda/\lambda^2 - 1)(\lambda - \sin\theta_1). \tag{21}$$

As might be expected, the time necessary to reach the
zero radius position is a function of the launch coordinates
as well as the penetration ability of the gliding system.
When θ_1 is taken as the independent variable, τ a non
dimensional time quantity as the radial position coordinate,
and λ considered to be a parameter, the plane curve generated by
(21) is recognized as a special form of the limacon of Pascal.

Figure (4) is a graphical presentation of equation (21).
Physically, the situation that is being considered, is the
case where a circle is imagined to be drawn about the
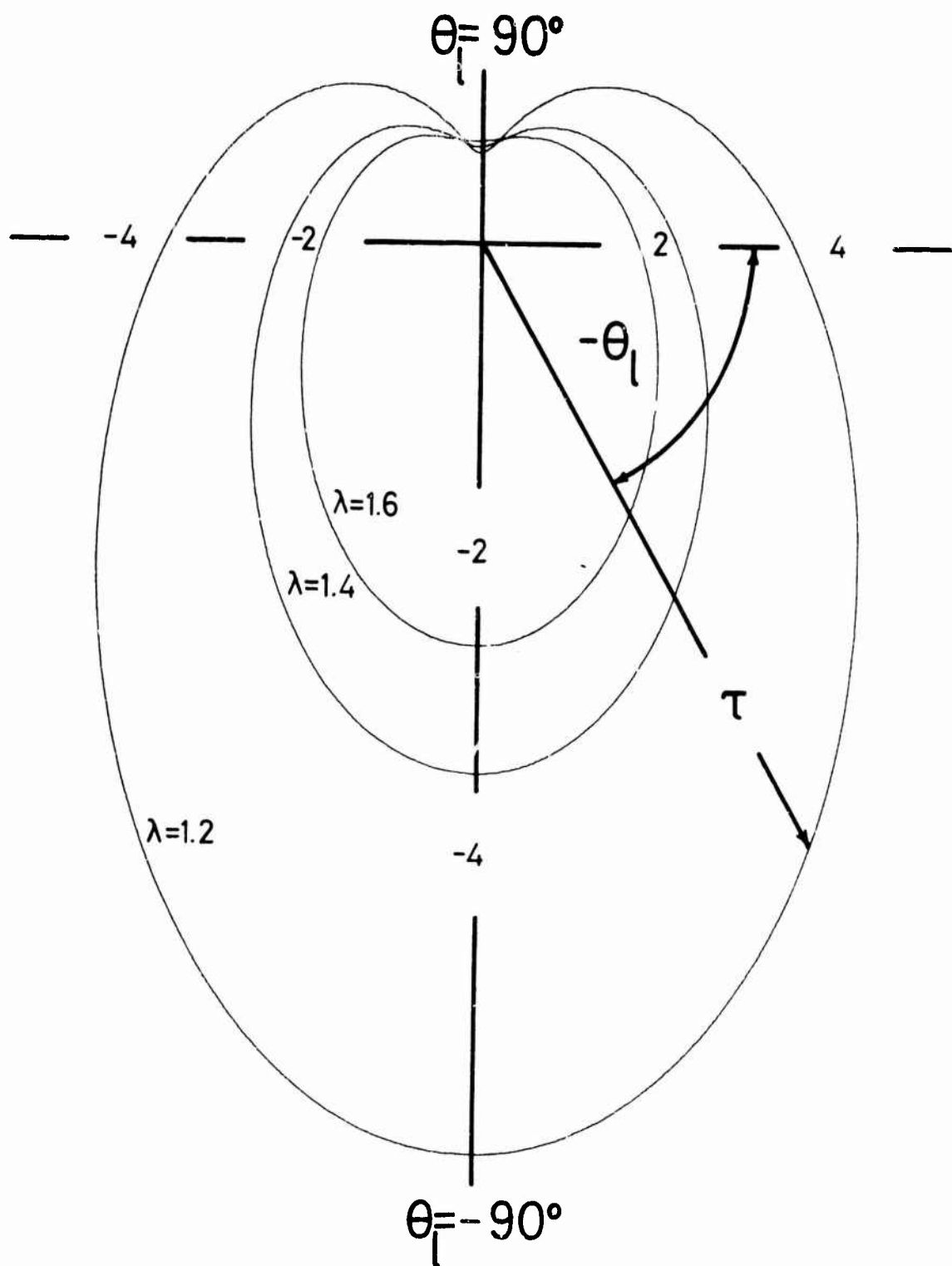
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FIGURE 4: FLIGHT TIME REQUIREMENTS FROM POSITIONS ON
A UNIT CIRCLE CENTERED AT THE IMPACT POINT.

intended impact point and the required flight time from various locations on the circumference is to be determined. In this discussion it is assumed, of course, that the launch is a premediatated one, and that the question of where to initiate the trajectory is being addressed. The form of (21) is a convenient one for handling this analysis since the quantities capable of independent variation will represent changes in wind heading and intensity. In practice it may be conceivable to exercise tight control over the in-flight positioning of the launch platform, as well as the sequence involving the deployment and inflation of the gliding device. However, control over environmental conditions obviously is beyond the realm of practical consideration. All that can reasonably be expected concerning the wind, is knowledge of its nominal magnitude and direction at some time close to the actual launch. The determining factor then regarding accuracy, will be the wind velocity. It is, therefore, extremely desirable if possible to select an initial launch position which is relatively insensitive to tolerable fluctuations in wind speed or direction.

From Figure (4) the manner in which the time of flight curves tend to flatten and collect near the 90 degree ray leads to the tentative conclusion that this is the optimum azimuth position. To substantiate this observation analytically, the change in τ due to independent variations in λ and θ_1 is investigated through equation (21). Consider then;

$$d\tau = (\partial\tau/\partial\lambda)d\lambda + (\partial\theta/\partial\theta_1)d\theta_1; \qquad (22)$$

Where,

$$(\partial\tau/\partial\lambda) = \{(\lambda^2+1)\sin\theta_1-2\lambda\}/(\lambda^2-1)^2. \qquad (23)$$

and,

$$(\partial\tau/\partial\theta_1) = -\lambda\cos\theta_1/(\lambda^2-1). \qquad (24)$$

The most desirable circumstance in (22) would be for $d\tau$ to be zero for all allowable variations in $d\lambda$ or $d\theta_1$. This requires both (23) and (24) to vanish simultaneously. However, for $\lambda > 1$ there is no unique launch azimuth which will satisfy this condition. The objective then will be to locate the value of θ_1 which makes the respective coefficients of $d\lambda$ and $d\theta_1$ as close to zero as possible. In this manner the absolute value of $d\tau$ is in a sense, minimized. To determine θ_1 the algebra of vectors and vector space will be useful. From equation (22) $d\tau$ can be thought of as a scalar quantity generated by the dot product of two vectors. These numerical vectors are derived in turn from the sensitivity coefficients $\partial\tau/\partial\lambda$ and $\partial\tau/\partial\theta_1$, and the error terms $d\lambda$ and $d\theta_1$. Utilizing this notion, the Schwartz inquality criterion[6] can be applied directly to equation (22) yielding the requirement that;

$$|d\tau| \leq \{(\partial\tau/\partial\lambda)^2+(\partial\tau/\partial\theta_1)^2\}^{1/2}\{(d\lambda)^2+(d\theta_1)^2\}^{1/2}. \qquad (25)$$

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From this result then it is seen that in order for $|d\tau|$ to remain small, while the direction and intensity of the wind is allowed to vary in an independent and uncontrollable fashion, the value of $\{(\partial\tau/\partial\lambda)^2+(\partial\tau/\partial\theta_1)^2\}^{1/2}$ must be minimum. This condition is met when θ_1 = 90 degrees for all positive $\lambda \lessdot 100$.

It has been established from the above discussion, that flight time requirements as determined from equation (21) for θ_1 = 90 degrees will be insensitive to minor wind anomalies. Since wind changes cannot be controlled or anticipated in the manner that other variables may be influenced, a release position accurately located according to this criterion will result in the smallest dispersions at the impact point.

Fixed Time of Flight

Again considering the case of a premediatated launch where $\lambda > 1$, the circumstance very often occurs where it is desirable to deliver multiple loads in some sequential fashion from a single launch vehicle. If a gliding decelerator homing according to some steering law, is employed for this application phasing of the individual deployments becomes critical. This problem can be addressed, that is in an analytical sense, by attempting to determine for the particular guidance routine being used, the locus of points about the target which have equal flight time. For the particular case of radial guidance, this curve can be generated by

requiring both t and λ to be fixed in (21) and solving for the launch radius r_1 in terms of θ_1.

When this is done, it is observed that;

$$r_1 = J/\{1-(1/\lambda)\sin\theta_1\} \quad ; \tag{26}$$

Where,

$$J \underline{\Delta} (ut)(\lambda^2-1)/\lambda^2 \quad . \tag{27}$$

Since $1/\lambda$ is always positive and less than 1 for all $\lambda>1$, and J is a positive constant, equation (26) is identified as the polar equation of an ellipse. The focus of the curve becomes the target and the wind line the major axis.

Equation (26) is a surprising and potentially useful result. Radial homing gliding systems whose trajectories are initiated at different points along this elliptical path will have equal flight time requirements relative to reaching their common aiming point. Consequently, when this launch profile is executed the time increment between successive items discharged from an aircraft in motion no longer becomes a significant factor affecting the dispersal of individual loads at the impact point.

CONCLUSIONS

The attributes of one type of steering technique used for guiding aerodynamic decelerators capable of independent motion through the air has been discussed by examining the close form solutions to the equations of motion when a constant

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wind velocity is assumed. Analysis of the trajectory equation
shows that except for perfect alignment along the wind line,
a gliding system maneuvering according to a radial aiming
scheme, must have a horizontal airspeed component greater
than the wind speed in order for it to reach the homing
transmitter prior to impact. This result essentially defines
the lift to drag requirements for the radial homing system
designed to function in some specified nominal or extreme
wind environment.

The parabolic ground track which occurs for the special
case where the magnitude of the parachute's intrinsic
velocity is precisely matched by the wind speed, is an in-
teresting result which may be useful in establishing physical
requirements for a target area. That is, assuming that a
particular gliding system will only be employed in conditions
where it can penetrate the wind and if tolerance limits are
then assigned to positioning errors at the release point,
along with estimates of wind variability in the time span
surrounding the mission, a region with high impact
probability can be determined from the trajectory of a
reference parabola derived from calculations based on the
extreme launch points.

Impact, particularly with high horizontal velocities,
is a problem of concern with any airdrop system. A very
desirable feature of the radial guidance scheme regarding its

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potential for attenuating velocities imparted by the wind
is the apparent stabilizing influence of the wind line. That
is, the interaction between the radial constraint and the
wind velocity essentially forces the system to seek alignment
into the wind, and resist disturbances from this position
once it is established. In effect, a natural mechanism is
provided which attempts to minimize the ground speed while
restricting the direction of the net horizontal motion to
one dimension.

Launch criteria, for radial homing systems have been
identified through analysis of the time solution derived
from basic considerations. Two developments have been
presented. The first deals with individual load accuracy,
and demonstrates that in order to minimize errors at the impact
point due to variations in wind velocity, the release point
should be located up-wind along the nominal wind axis. Since
no physical control over the wind velocity is possible, this
result establishes the optimum launch position. The second
development, addresses the circumstance requiring the delivery
of multiple loads which are individually discharged from a
single vehicle at discrete points along its flight track.
In this case, the problem is expanded from the determination
of a single release point to the determination of a release
path. For the radial steering procedure an elliptical path,

derived from nominal wind conditions will define the locus
of points from which the flight time necessary to reach the
target is constant. That is, the ability to land at the
designated impact point is independent of the launch position
along this curve. From this result a flight program can be
developed for the accurate delivery of multiple loads.

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